

# The Determination of Mass Transfer Characteristics of a Column for Sulphur Dioxide Adsorption in 13 X Zeolite Working in Unsteady-State Regime

IRINA PINCOVSCI<sup>1</sup>, CRISTINA MODROGAN<sup>2\*</sup>

<sup>1</sup>University Politehnica of Bucharest, Department of Hydraulics, Hydraulic Machinery and Environmental Engineering, 1-7 Gh. Polizu Str., 011061, Bucharest, Romania

<sup>2</sup>University Politehnica of Bucharest, Department of Analytical Chemistry and Environmental Engineering, 1-7 Gh. Polizu Str., 011061, Bucharest, Romania

*In the present work, the mass transfer characteristics such as the length of mass transfer unit ( $L_{MTU}$ ), the break through time and column saturation time have been studied in the case of sulphur dioxide adsorption on 13 X zeolite. The adsorption column was working in unsteady-state conditions. For these determinations a chromatographic method has been used, permitting the direct inregistration of breakthrough curves, whose shape depends on adsorption conditions (gas concentration, temperature, the size of adsorbent grains, gas velocity). The method is very sensitive, reflecting all changes of adsorption parameters.*

**Keywords:** zeolites; adsorption in unsteady-states regime; mass transfer unit; breakthrough curves

Large combustion plants contribute greatly to emissions of sulfur dioxide, nitrogen oxides and dust, so it is necessary to reduce these emissions to the requirements of the best available techniques [1, 2].

In a previous paper [3, 4] a chromatographic method has been presented permitting the direct obtention of breakthrough curves. The main advantages of this method are his sensitivity and the possibility to reflect continuously all the changes of adsorption parameters.

The determination of breakthrough curve has been studied using theoretical models [3-14] and practical methods as well [15-24].

The theoretical models developed for determination of breakthrough curves in adsorption columns working in unsteady-state regime are generally based on the following assumptions:

- the temperature remains practically constant throughout the adsorption bed;
- the pressure-drop along the bed is negligible under the experimental conditions;
- there is a constant fluid velocity throughout the bed.

Different adsorption models are presented in literature: pore diffusion model, surface diffusion model and bidispersed diffusion model.

The pore diffusion model can be considered when diffusion occurs in the macro and mesoporous adsorbents.

In the surface diffusion model the diffusing molecules can not escape the force field of adsorbent surface. The surface diffusivity coefficient is generally much smaller than the other diffusivities.

In the bidispersaed diffusion model the macropore and micropore diffusion control the mass transfer simultaneously.

In the literature has been also proposed the pore diffusion with kinetic isotherm. This model is the same as pore diffusion model except that no equilibrium exist between pore and solid.

In all adsorption studies the two cases have been taken in consideration: single component adsorption and multicomponent adsorption. In the first case all mentioned models have been used. In the second case the extended Langmuir isotherm model has been also applied.

The most difficulties in using the mentioned theoretical model consist in adoption of a lot of simplifying assumption. That is why the theoretical breakthrough curves do not reflect exactly all changes of adsorption parameters.

The chromatographic method used in the present work put in evidence continuously all the adsorption conditions and the accidentally changes of adsorption parameters [4].

## Experimental part

In this work the 13X zeolite have been used as adsorbent. Two electronic controllers have been used for measure the flowrates of SO<sub>2</sub> and N<sub>2</sub>. The two individual streams were mixed in a mixing chamber.

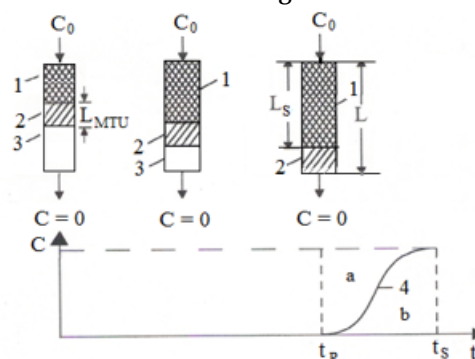


Fig. 1. The physical model used for the gas adsorption process in unsteady-state regime. 1 - the saturated zone; 2- the length of the mass transfer unit ( $L_{MTU}$ ); 3- the free zone; 4- the breakthrough curve;  $t_R$  -the breakthrough time;  $t_S$  - column saturation time;  $C_0$  -initial gas concentration

After mixing chamber, the gas having the concentration  $C_0$  passes through the adsorption column (being of 2 cm diameter and 40 cm high). The proposed physical model is based on the assumption that the gas adsorption occurs till the saturation of a limited zone  $L$ , defined as mass transfer unit ( $L_{MTU}$ ), whose length depends on adsorption conditions (gas concentration, temperature, adsorbent granule size, gas velocity). When the mass transfer unit attains the final outlet position, the gas concentration is continuously increased from  $C = 0$  to  $C = C_0$  in accordance with breakthrough curve 4 (fig. 1). That she is why the

\*email: c\_modrogan@yahoo.com

breakthrough curve characterizes the adsorption process in unsteady-state conditions, permitting the calculation of all characteristic parameters (the length of mass transfer unit, the adsorption degree in dynamic conditions, the optimum number of  $L_{MTU}$  and therefore the optimum adsorption column length).

The breakthrough curve is continuously recorded using the chromatographic device presented in figure 2 [4].

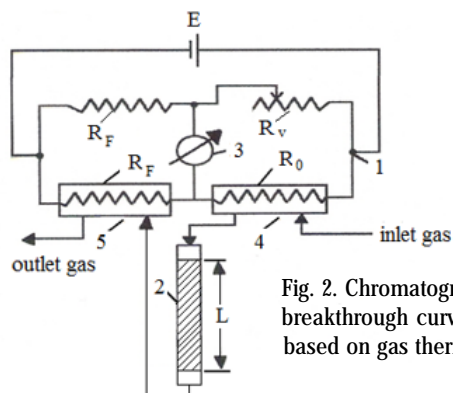


Fig. 2. Chromatographic device for breakthrough curve determination based on gas thermal conductivity

1 - chromatographic device; 2- adsorption column; 3- recorder;  $R_0$ -platinum electric resistance;  $R_i$  - reference platinum electric resistance;  $R_F$  - fixed manganine electric resistance;  $R_v$ -variable manganine electric resistance

The gas containing sulfur dioxide, whose initial concentration is  $C_0$ , enters successively the aluminium channel 4 containing the electrical resistance  $R_0$ , adsorption column 2 and aluminium channel 5 containing the resistance  $R_F$ . Due to continue  $SO_2$  adsorption in column 2, its concentration continuously diminished, modifying the thermal conductivity of gas. This modification is recorded by the recorder 3, resulting the breakthrough curve.

Although the thermal conductivity of  $SO_2$  is relatively small one (the thermal conductivity  $l$  of sulfur dioxide, at 25 C, is  $2.08 \times 10^{-5}$  cal/cm . s . grd) the chromatographic device is sensitive enough for breakthrough curve recording. It is evident that the sensitivity of device increases with the increasing of  $SO_2$  concentration.

In the present work the following data have been used:  $C_0 = 0.25, 0.5$  and  $1\%SO_2$ ; the temperature was about 25 C; the grain size was about 1 mm and the gas velocity 0.4 m/s. The adsorbent was a commercial 13X zeolite.

## Results and discussions

Using the chromatographic device presented in figure 2 the breakthrough curves have been obtained for different parameters, permitting the calculation of the length of mass transfer unit ( $L_{MTU}$ ) the adsorption degree  $\theta_R$  in dynamic conditions, the breakthrough time  $t_R$ , the column saturation time  $t_s$  and the adsorption coefficient  $f = \frac{a}{a+b}$  (fig.1).

In order to determine the length of mass transfer unit ( $L_{MTU}$ ) the following relation has been used [1].

$$L_{MTU} = L \frac{t_s - t_R}{t_s - t_F} = L \frac{t_E}{t_s - t_E(1-f)} \quad (1)$$

where:  $L$  represents the length of adsorption column, cm

$t_s$  - the necessary time for column saturation, min

$t_R$  - the breakthrough time, min

$t_E$  - the time of displacement of  $L_{MTU}$ , min

$t_F$  - the formation time of  $L_{MTU}$ , min

$f$  - the adsorption coefficient

Knowing the  $L_{MTU}$ , the adsorption degree  $\theta_R$  in breakthrough time  $t_R$  can be determined, according to the relation:

$$\theta_R = \frac{G_R}{a_m L} \quad (2)$$

where:

$G_R$  represents the quantity of  $SO_2$  retained in breakthrough time, kmol

$a_m$  - the linear concentration of  $SO_2$  adsorbed in time  $t_s$ , kmol/cm

The data contained in the breakthrough curve put in evidence that:

$$G_R = a_m L_S + a_m f L_{MTU} = a_m (L_S + f L_{MTU}) = a_m [L - L_{MTU}(1-f)]$$

where:  $L_S = L - L_{MTU}$  and (fig. 1)

In these conditions:

$$\theta_R = \frac{G_R}{a_m L} = \frac{a_m [L - L_{MTU}(1-f)]}{a_m L} = 1 - \frac{L_{MTU}(1-f)}{L} \quad (3)$$

The relation (3) puts in evidence the dependence of adsorption degree  $\theta_R$  on adsorption coefficient  $f$  and  $L_{MTU}$ . The adsorption conditions (the initial gas concentration  $C_0$ , the temperature, the size of adsorbent grains, the gas velocity) must ensure a big value of  $f$  and a small one for  $L_{MTU}$ , as results from equation (3) written as follows:

$$\theta_R = 1 - \frac{L_{MTU}(1-f)}{n L_{MTU}} = 1 - \frac{1-f}{n} \quad (3')$$

where:  $n$  represent the number of  $L_{MTU}$  in a column having the length  $L$ .

The figure 3 represents the dependence of adsorption degree  $\theta_R$  on the number of  $L_{MTU}$  for two adsorption coefficients  $f$  (0.4 and 0.6).

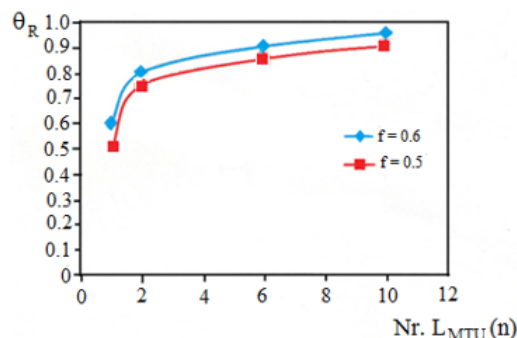


Fig. 3. Variation of the degree of adsorption  $\theta_R$  on the number  $n$  of mass transfer units at different values of the coefficient of adsorption

In order to obtain big values for  $\theta_R$  the number of  $L_{MTU}$  must be sufficiently high. According to the relation  $L = n \cdot L_{MTU}$ , the adsorption conditions must ensure small values for  $L_{MTU}$ . That is very important from economical and technical reasons, because increasing the number of  $L_{MTU}$  the pressure drop increases as well.

*The influence of initial gas concentration  $C_0$  on  $L_{MTU}$*

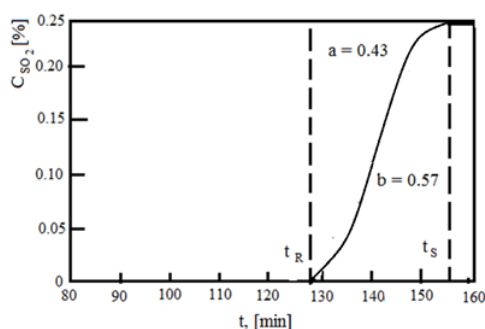


Fig. 4. The shape of breakthrough curve when  $C_0 = 0.25\% SO_2$

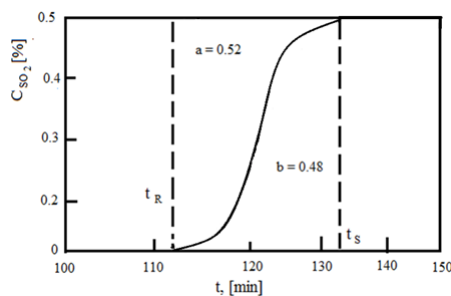


Fig. 5. The shape of breakthrough curve when  $C_0 = 0.5\% \text{ SO}_2$

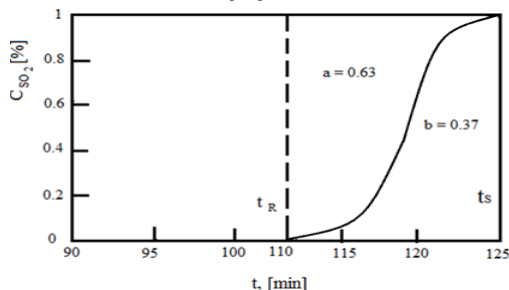


Fig. 6. The shape of breakthrough curve when  $C_0 = 1\% \text{ SO}_2$

In order to put in evidence the influence of  $C_0$  on  $L_{MTU}$ , the breakthrough curves have been obtained for  $C_0 = 0.25; 0.5$  and  $1\% \text{ SO}_2$ . These curves are represented in the figures 4, 5 and 6 respectively.

In all cases the experiences have been performed in a column where the adsorbent length  $L = 40 \text{ cm}$  (diameter =  $3 \text{ cm}$ ).

The gas velocity was  $w_g = 0.2 \text{ m/s}$ . The grain diameter of adsorbant  $d_p = 1 \text{ mm}$ .

For the initial gas concentration  $C_0 = 0.25\%$ , the column saturation time  $t_s = 155 \text{ min}$  and the breakthrough time  $t_R = 127 \text{ min}$ .

In this case the displacement time of  $L_{MTU}$ ,  $t_E = t_s - t_R = 155 - 127 = 28 \text{ min}$  and the formation time of  $L_{MTU}$ ,  $t_F = t_E (1-f) = 28 (1-0.38) = 17 \text{ min}$ .

In these conditions:

$$\theta_R = \frac{G_R}{a_m L} = \frac{a_m [L - L_{MTU}(1-f)]}{a_m L} = 1 - \frac{L_{MTU}(1-f)}{L}$$

For the initial concentration  $C_0 = 0.5\%$  the data are the following:  $t_s = 132 \text{ min}$ ;  $t_R = 113 \text{ min}$ ;  $t_E = t_s - t_R = 132 - 113 = 19 \text{ min}$

$$t_F = t_E (1-f) = 19 (1-0.42) = 11$$

In these conditions:

$$L_{MTU} = L \frac{t_E}{t_s - t_F} = 40 \frac{19}{132 - 11} = 7.4 \text{ cm}$$

Finally, when  $C_0 = 1\%$  the data are the following:

$t_s = 125 \text{ min}$ ;  $t_R = 111 \text{ min}$ ;  $t_E = 125 - 111 = 14 \text{ min}$ ;  $t_F = 14 \times (1-0.52) = 6.7 \text{ min}$ .

One obtains:

$$L_{MTU} = L \frac{t_E}{t_s - t_F} = 40 \frac{14}{125 - 6.7} = 4.6 \text{ cm}$$

As aspected, the  $L_{MTU}$  increases when the initial concentration  $C_0$  decreases. That why the purification of very diluted gases may become very expensive, the big pressure drop becoming unacceptable.

The variation of  $L_{MTU}$  with  $C_0$  is represented in figure 7.

The experiments made in order to put in evidence the influence of temperatures, gas velocities and the size of adsorbent grains on  $L_{MTU}$  confirm the previsible facts that small temperatures, gas velocity and grain dimensions are favorable to obtain small values for  $L_{MTU}$ . Unfortunately

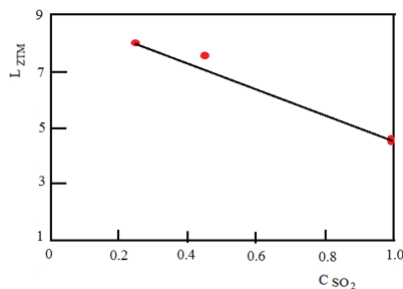


Fig. 7. The variation of mass transfer unit length with the concentration of  $\text{SO}_2$

small values of these parameters are prohibitive from practical point of view.

## Conclusions

The aim of this work is the determination of mass transfer characteristics, such as the length of mass transfer unit ( $L_{MTU}$ ), the breakthrough time  $t_R$  and the column saturation time  $t_s$ , which permit finally the calculation of adsorption coefficient in unsteady-state conditions  $q_R$ , and of the optimum number  $n$  of  $L_{MTU}$ . In this purpose a chromatographic method has been used, permitting the direct inregistration of breakthrough curves, whose shape depends on adsorption parameters like gas concentration, temperature, the size of adsorbent grains and the gas velocity.

## References

- BUMBAC, G., BOMBOS, D., Rev. Chim. (Bucharest), **66**, no. 11, 2015 p. 1891
- CAPATINA, C., CIRTINA, D., Rev. Chim. (Bucharest), **68**, no. 10, 2017, p. 2248
- ORBULET, O.D., PINCOVSCHI, I., MODROGAN C., Rev. Chim. (Bucharest), **67**, no. 5, 2016, p. 829
- PINCOVSCHI, I., MODROGAN, C., Rev. Chim. (Bucharest), **65**, no. 8, 2014, p. 876
- GUPTA, A., GAUR, V., VERNA, N., Chem. Eng. And Processing, **43** (2004), p.9
- SIAPPOOSH, M., FAYTEMI, S., VATANI, A., Iran. J. Chem. Chem Eng., **28** (2009), p. 25
- YOON, Y., NELSON, J.H., An. Ind. Hyg. Assoc. J., **45** (1994), p. 509
- CARTA, G., CINCOTTI, A., Chem. Eng.Sci., **53** (1998), p. 3483
- ZHANG, R., RITTER, J.A., Chem. Eng. Sci. **52** (1977), p. 3161
- SCRBEZOV, A., SOTIRCHOS, J.A., Chem. Eng.Sci., **54** (1999), p. 5647
- WAKAO, N., FUNAZKRI, T., Chem. Eng.Sci., **33** (1978), p. 1375
- FAROOK, S., RUTHVEN, M., AICh. Journal, **37** (1991) p. 299
- THIBAUT-ERKEY, C., GUO, Y., ERKEY, C., AKGERMAN, A., Environ. Sci. Technol. **30** (1996) p. 2127
- KOPAC, T., Chem. Eng. and Process., **38** (1999) p. 45
- MIHALY, M., ANDREIADIS, E.S., PINCOVSCHI, E., UPB Sci. Bull., Series B, vol. **67** (2005), p. 57
- CHANG, C.L., CHIANG, P.C., CHANG, E.E., Chemosphere, **53** (2003) p. 17
- SANKARARAO, B., GUPTA, S.K., Comp. Chem. Eng., **31** (2007), p. 1282
- VERMULEN, T., QUILICI, I., Ind. Eng. Chem. Fundam. **9** (1970), p. 179
- CHANG, H., YUAN, X., TIAN, H., ZENG, A., Chem. Eng. and Process, **45** (2006) p. 747
- TANTET, J., EIC, M., DESAI, R., Gas. Sep. Purif. **9** (1995) p. 233
- GAUR, V., SHARMA, A., VERMA, N., Chem. Eng. and Process., **45** (2006) p. 1
- KOPAC, T., KOCABAS, S., Chem. Eng. and Process., **41** (2002) p. 223
- LEE, Y.W., PARK, J.W., CHOUNG, J.H., CHOI, D.K., Environ. Sci. Technol., **36** (2002) p. 1086
- IGHIGEANU, D., MARTIN, D., CALINESCU, I., BULEARCA, A., MANAILA, E., CRACIUN, G., Rev. Chim. (Bucharest), **63**, no. 2, 2012, p. 187

Manuscript received: 23.11.2017